

NJR/KS/18/3228**Bachelor of Computer Application (B.C.A.) Semester-III (C.B.S.) Examination****OPERATIONS RESEARCH-I****Paper-IV**

Time : Three Hours]

[Maximum Marks : 50

N.B. :— (1) **All** questions are compulsory and carry equal marks.

(2) Draw neat and labelled diagrams wherever necessary.

EITHER

1. (A) Explain significant features of operation research. 5
- (B) Two different types of foods 'A' and 'B' are being considered to form a weekly diet. The minimum weekly requirements for fats carbohydrates and protein are 18, 24 and 16 units respectively. One kg. of food 'A' has 4, 16 and 8 units respectively of these ingredients and one kg. of Food 'B' has 12, 4 and 6 units respectively. The price of food 'A' is Rs. 6 per kg and that of food 'B' is Rs. 5 per kg. How many kg. of each type of food should be buy per week to minimize the cost and meet these requirements. Formulate this as L.P.P. 5

OR

- (C) Explain the phases of operation research. 5
- (D) Solve the following L.P.P. by graphical method :

$$\text{Maximize } Z = 4x_1 + 3x_2$$

subject to the constraints

$$2x_1 + x_2 \leq 1000 ; x_1 + x_2 \leq 800 ;$$

$$x_1 \leq 400 ; x_2 \leq 700 \text{ and } x_1, x_2 \geq 0. \quad 5$$

EITHER

2. (A) Solve the following L.P.P. using Simplex method :

$$\text{Maximize } Z = 3x_1 + 2x_2$$

subject to the constraints :

$$x_1 + x_2 \leq 3$$

$$x_1 \leq 2$$

$$-2x_1 + x_2 \leq 1$$

$$\text{and } x_1, x_2 \geq 0. \quad 5$$

- (B) Give the steps for formulating a dual problem of a primal problem. 5

OR

- (C) Use penalty method (Big-M) to :

$$\text{Maximize } Z = 2x_1 + 3x_2$$

subject to the constraints :

$$x_1 + 2x_2 \leq 4$$

$$x_1 + x_2 = 3$$

$$\text{and } x_1, x_2 \geq 0. \quad 5$$

(D) Obtain the dual of L.P.P. :

$$\text{Minimize } Z = 4x_1 + 6x_2 + 18x_3$$

subject to the constraints :

$$x_1 + 3x_2 \geq 3$$

$$x_2 + 2x_3 \geq 5$$

$$\text{and } x_j \geq 0 \quad (j = 1, 2, 3).$$

5

EITHER

3. (A) Explain mathematical model for transportation problem.

5

(B) Solve the following transportation problem using Vogel's approximation method :

Source	Destination			Availability
	1	2	3	
1	20	22	40	100
2	24	35	17	150
3	32	30	10	125
Requirements	75	125	175	

5

OR

(C) Write down an algorithm for least-cost method.

5

(D) What is unbalanced transportation problem ?

Solve the following transportation problem :

	Destination				Supply
	1	2	3	4	
A	4	6	8	13	50
B	13	11	10	8	70
C	14	4	10	13	30
D	9	11	13	8	50
Demand	25	35	105	20	

5

EITHER

4. (A) Define assignment problem and give the mathematical formulation of the assignment problem.

5

(B) Solve the following assignment problem :

Jobs	Workers			
	W	X	Y	Z
A	8	7	9	10
B	7	9	9	8
C	10	8	7	11
D	10	6	8	7

5

OR

(C) Explain Branch and Bound technique to solve assignment problem. 5

(D) Solve the following assignment problem to minimize the cost of assignment :

$$\text{Cost Matrix : } \begin{bmatrix} 8 & 7 & 6 \\ 5 & 7 & 8 \\ 6 & 8 & 7 \end{bmatrix} \quad 5$$

5. Attempt **all** :

(A) Give the classification of models in operations research. 2½

(B) Write the following L.P.P. in standard form :

$$\text{Maximize } Z = 4x_1 + 5x_2$$

subject to the constraints ;

$$6x_1 + 5x_2 \leq 250 ; \quad 6x_1 + 5x_2 \geq 150 ;$$

$$4x_1 + 6x_2 \leq 200 ; \quad 9x_1 + 5x_2 \geq 130 ;$$

and $x_1, x_2 \geq 0$. <http://www.rtmnuonline.com> 2½

(C) Explain North-West corner rule to find initial basic feasible solution of T.P. 2½

(D) Draw the associated network for the following assignment table :

$$\begin{array}{c} \mathbf{W}_1 \\ \mathbf{W}_2 \\ \mathbf{W}_3 \end{array} \begin{array}{ccc} \mathbf{J}_1 & \mathbf{J}_2 & \mathbf{J}_3 \\ \begin{bmatrix} 12 & 22 & 30 \\ 20 & 9 & 15 \\ 17 & 25 & 10 \end{bmatrix} \end{array} \quad 2\frac{1}{2}$$