

$$\mathbf{F} = \mathbf{F} + \mathbf{F} +$$

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Using Sylvester's theorem, verify $\log_e e^A = A$ where $A = \begin{bmatrix} 0 & 1 \\ -2 & 3 \end{bmatrix}$

- b) Reduce the quadratic form $3x^2 + 3y^2 + 3z^2 + 2xy + 2xz 2yz$ to the canonical form by orthogonal transformation.
- c) Solve the differential equation 1^2

$$\frac{d^{2}x}{dt^{2}} + 5\frac{dx}{dt} + 6x = 0, \ x(0) = 2$$
$$x'(0) = 0$$

by matrix method.

The content of urn I, II, III are as follows : 2 white, 2 black, 3 red, 2 white, 1 black, 1 red and 4 white, 5 black, 3 red balls respectively. One urn is chosen at random and two balls drawn, they happen tobe white and red. What is the probability that they come from urn I?

b) A random variable X has the density function

$$f(x) = \begin{cases} cx^2, & 1 \le x \le 2\\ cx, & 2 < x < 3\\ 0, & otherwise \end{cases}$$

Find (i) constant C (ii) P(X > 2) (iii) $P\left(\frac{1}{2} < x < \frac{3}{2}\right)$.

OR

10. a)

a)

The joint probability function of X and Y is given by $f(x, y) = \begin{cases} c(2x + y), & x = 0, 1, 2\\ 0, & y = 0, 1, 2, 3\\ 0, & Otherwise \end{cases}$

Find (i) constant C (ii) $P(x \ge 1, y \le 2)$ (iii) The marginal probability function of X and Y.

b) Find the conditional density function of (i) X given Y (ii) Y given X for the distribution function.

 $f(x, y) = \begin{cases} \frac{3(x^2 + y^2)}{2}, & 0 \le x \le 1\\ 0, & 0 \le y \le 1\\ 0, & \text{otherwise} \end{cases}$

11. a) A random variable X is expected value of $E\left[(X-1)^2\right] = 10$ and $E\left[(X-2)^2\right] = 6$ find (i) E(X) (ii) Var (X) (iii) σ_x S.D. of x.

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